

# Mark Scheme (Results)

January 2025

Pearson Edexcel International Advanced Level In Mechanics M2 (WME02) Paper 01

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#### **General Marking Guidance**

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

## **EDEXCEL IAL MATHEMATICS**

## **General Instructions for Marking**

- 1. The total number of marks for the paper is 75.
- 2. The Edexcel Mathematics mark schemes use the following types of marks:
- **M** marks: Method marks are awarded for `knowing a method and

attempting to apply it', unless otherwise indicated.

- A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- **B** marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.
- 3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes and can be used if you are using the annotation facility on ePEN.

- bod benefit of doubt
- ft follow through
- the symbol  $\sqrt{}$  will be used for correct ft
- cao correct answer only
- cso correct solution only. There must be no errors in this part of the question to obtain this mark
- isw ignore subsequent working
- awrt answers which round to
- SC: special case
- oe or equivalent (and appropriate)
- d... or dep dependent
- indep independent
- dp decimal places
- sf significant figures
- \* The answer is printed on the paper or ag- answer given
- \_ or d... The second mark is dependent on gaining the first mark

- 4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.
- 5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected. If you are using the annotation facility on ePEN, indicate this action by `MR' in the body of the script.
- 6. If a candidate makes more than one attempt at any question:
  - If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
  - If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.
- 7. Ignore wrong working or incorrect statements following a correct answer.

## **General Principles for Mechanics Marking**

(NB specific mark schemes may sometimes override these general principles)

- Rules for M marks:
  - correct no. of terms
  - dimensionally correct
  - all terms that need resolving (i.e. multiplied by cos or sin) are resolved.
- Omission or extra g in a resolution is an accuracy error not method error.
- Omission of mass from a resolution is a method error.
- Omission of a length from a moments equation is a method error.
- Omission of units or incorrect units is not (usually) counted as an accuracy error.
- DM indicates a dependent method mark, i.e. one that can only be awarded if a previous specified method mark has been awarded.
- Any numerical answer which comes from use of g = 9.8 should be given to 2 or 3 SF.
- Use of g = 9.81 should be penalised once per (complete) question.
  - N.B. Over-accuracy or under-accuracy of correct answers should only be penalised *once* per complete question. However, premature approximation should be penalised every time it occurs.
- Marks must be entered in the same order as they appear on the mark scheme.
- In all cases, if the candidate clearly labels their working under a particular part of a question i.e. (a) or (b) or (c)...then that working can only score marks for that part of the question.
- Accept column vectors in all cases.
- Misreads if a misread does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, bearing in mind that after a misread, the subsequent A marks affected are treated as A ft

## **Mechanics Abbreviations**

| M(A) | Taking moments about A                             |
|------|--|
| N2L  | Newton's Second Law (Equation of Motion)           |
| NEL  | Newton's Experimental Law (Newton's Law of Impact) |
| HL   | Hooke's Law  |
| SHM  | Simple harmonic motion                             |
| PCLM | Principle of conservation of linear momentum       |
| RHS  | Right hand side                                    |
| LHS  | Left hand side                                     |

| 1. | Gain in GPE<br>= $2.6g \times 20 \sin \alpha \left( = 2.6g \times 20 \times \frac{5}{13} \right)$              | M1         | Or equivalent. Condone sine / cosine confusion  |
|----|--|------------|---|
|    | $F_{\max} = \frac{1}{5} \times 2.6g \cos \alpha \left( = \frac{1}{5} \times 2.6g \times \frac{12}{13} \right)$ | M1         | Or equivalent. Condone sine / cosine confusion  |
|    | Work done against friction = $20F_{max}$   | M1         | Follow their $F_{max}$ . Must have an expression for $F_{max}$ .<br>Independent of the preceding M1 |
|    | Total work done<br>= $2.6g \times 20 \sin \alpha + 4 \times 2.6g \cos \alpha$                                  | DM1        | Dependent on preceding M marks<br>Must be adding the two relevant<br>expressions                    |
|    | = 290(J)   | A1         | 2 sf or 3 sf<br>Do not ISW  |
|    |  |            | NB: Omission of g should be marked as an accuracy error   |
|    |  | [5]<br>(5) |   |
|    |  |            |   |

| 2a | NB If they use $a = 0$ then max score is $1/7$   | / (3 <sup>rd</sup> M | 1 only)   |
|----|--|----------------------|---|
|    | Equation of motion for van + trailer:  | M1                   | First equation: Dimensionally correct. Need all terms. In $F$ or $P$ . Condone sign errors.   |
|    | F - (500 + 200) = (900 + 300)a   | A1                   | Correct unsimplified equation   |
|    | Equation of motion for the trailer   | M1                   | Second equation: Dimensionally<br>correct. Need all terms. In <i>F</i> or <i>P</i> .<br>Condone sign errors. Correct mass   |
|    | T - 200 = 300a   | A1                   | Correct unsimplified equation.<br>Follow their <i>a</i> .   |
|    | Equation of motion for van $F - T - 500 = 900a$  |                      | There are 3 possible equations.<br>They need 2 of them. M1A1 for<br>each correct unsimplified<br>equation.  |
|    | $F = \frac{18000}{12} (=1500)$   | M1                   | Use of $P = Fv$ Need to have<br>substituted relevant values<br>Condone use of 18 in place of<br>18000 (or incorrect number of<br>zeros)   |
|    | Solve for <i>T</i>   | DM1                  | Dependent on previous 3 M marks   |
|    | T = 400  | A1                   | Correct only  |
|    |  |                      | NB: Inclusion of g should be  |
|    |  |                      | marked as an accuracy error   |
|    |  | [7]                  |   |
| 2b | Equation of motion for van + trailer   | M1                   | Dimensionally correct. Need all<br>terms. Condone sign errors.<br>Condone sine / cosine confusion<br>Alt: Obtains separate equations for<br>van and trailer and eliminates <i>T</i>   |
|    | $F - (200 + 500) - (300 + 900)g\sin\alpha = 0$ $\left(\frac{18000}{v} = 700 + \frac{1200g}{15}\right)$ | A1<br>A1             | Unsimplified equation in $F$ or $v$<br>with at most one error. Consistent<br>trig confusion is one error.<br>Consistent sign error is one error.<br>Missing $g$ is one error.<br>Correct unsimplified equation in $v$<br>Allow with trig value not<br>substituted |
|    | v = 12  or  v = 12.1   | A1                   | 2 sf or 3 sf  |
|    |  | [4]                  |   |
|    |  | (11)                 |   |
|    |  |                      |   |

| 3a | Use $\mathbf{v} = \frac{\mathbf{d}\mathbf{r}}{\mathbf{d}t}$  | M1                                | Differentiate the vector. At least 3 powers going down   |
|----|--|-----------------------------------|--|
|    | $\mathbf{v} = \left(3 - \left(t + 1\right)^{-\frac{1}{2}}\right)\mathbf{i} + \left(2t - 6\right)\mathbf{j}$  | A1<br>A1                          | one component correct<br>both components correct.  |
|    | $(2t-6) = 0 \Longrightarrow t = 3$   | M1                                | Equate their <b>j</b> component of<br>velocity to zero and solve for <i>t</i><br>Must have seen a clear attempt to<br>differentiate  |
|    | Speed = $2.5(ms^{-1})$ or equivalent   | A1                                | Must be a scalar. A0 for 2.5i  |
|    |  | [5]                               |  |
|    |  |                                   |  |
| 3b | Use $\mathbf{a} = \frac{\mathrm{d}\mathbf{v}}{\mathrm{d}t}$  | M1                                | Differentiate the vector. Powers<br>going down and at least one<br>constant goes to zero.  |
|    | $\mathbf{a} = \frac{1}{2} (t+1)^{-\frac{3}{2}} \mathbf{i} + 2\mathbf{j}$   | A1                                | Or equivalent correct expression<br>Allow if correct derivative<br>implied by correct substitution   |
|    | $\left(\mathbf{a} = \frac{4}{\sqrt{125}}\mathbf{i} + 2\mathbf{j}\right) \left \mathbf{a}\right  = \sqrt{\frac{16}{125} + 2^2}$   | DM1                               | Correct use of Pythagoras<br>Dependent on the preceding M1   |
|    | $= 2.03 \left( m s^{-2} \right)$ or better   | A1                                | $\frac{2\sqrt{645}}{25}$ or 2.0317   |
|    |  | [4]                               |  |
| 3c | For $\mathbf{r} = 0, (3t + 2 - 2\sqrt{t+1}) = 0$ and   | M1                                | No need to consider $t = 0$ as this is   |
|    | $(t^2 - 6t) = 0$   |                                   | excluded in the Q  |
|    |  | A1                                | Clear explanation of the given result with no errors seen.   |
|    | $(t^2 - 6t) = 0$<br>$t \neq 0 \Longrightarrow t = 6$ but $(3 \times 6 + 2 - 2\sqrt{6+1}) \neq 0$<br>Hence no solution and does not return  | A1                                | Clear explanation of the given   |
|    | $(t^{2} - 6t) = 0$ $t \neq 0 \Longrightarrow t = 6 \text{ but } (3 \times 6 + 2 - 2\sqrt{6 + 1}) \neq 0$   | f the ve<br>clusion               | Clear explanation of the given<br>result with no errors seen.<br>e.g. $(3t+2-2\sqrt{t+1})=0$<br>$\Rightarrow 9t^2+8t=0$ has no solution for<br>t > 0 (need something to indicate<br>impossible)<br>locity is always > 2, so no return<br>with no errors seen and sufficient  |
|    | $(t^2 - 6t) = 0$<br>$t \neq 0 \Rightarrow t = 6$ but $(3 \times 6 + 2 - 2\sqrt{6+1}) \neq 0$<br>Hence no solution and does not return<br>There will be other alternatives<br>e.g. Show that the horizontal component of<br>M1 for correct strategy A1 for correct con-<br>justification. Conclusion needs to be clear  | of the ve<br>clusion<br>t but doe | Clear explanation of the given<br>result with no errors seen.<br>e.g. $(3t+2-2\sqrt{t+1})=0$<br>$\Rightarrow 9t^2+8t=0$ has no solution for<br>t > 0 (need something to indicate<br>impossible)<br>locity is always > 2, so no return<br>with no errors seen and sufficient<br>es not need to be the exact wording |
|    | $(t^2 - 6t) = 0$<br>$t \neq 0 \Rightarrow t = 6$ but $(3 \times 6 + 2 - 2\sqrt{6+1}) \neq 0$<br>Hence no solution and does not return<br>There will be other alternatives<br>e.g. Show that the horizontal component of<br>M1 for correct strategy A1 for correct con<br>justification. Conclusion needs to be clean<br>from the question.<br>An argument dependent solely on acceleration | of the ve<br>clusion<br>t but doe | Clear explanation of the given<br>result with no errors seen.<br>e.g. $(3t+2-2\sqrt{t+1})=0$<br>$\Rightarrow 9t^2+8t=0$ has no solution for<br>t > 0 (need something to indicate<br>impossible)<br>locity is always > 2, so no return<br>with no errors seen and sufficient<br>es not need to be the exact wording |
|    | $(t^2 - 6t) = 0$<br>$t \neq 0 \Rightarrow t = 6$ but $(3 \times 6 + 2 - 2\sqrt{6+1}) \neq 0$<br>Hence no solution and does not return<br>There will be other alternatives<br>e.g. Show that the horizontal component of<br>M1 for correct strategy A1 for correct con<br>justification. Conclusion needs to be clean<br>from the question.<br>An argument dependent solely on acceleration | f the ve<br>clusion<br>but doe    | Clear explanation of the given<br>result with no errors seen.<br>e.g. $(3t+2-2\sqrt{t+1})=0$<br>$\Rightarrow 9t^2+8t=0$ has no solution for<br>t > 0 (need something to indicate<br>impossible)<br>locity is always > 2, so no return<br>with no errors seen and sufficient<br>es not need to be the exact wording |

| 4         | NB: For the whole of this question, confusion between horizontal and vertical is <b>not</b> |      |  |  |
|-----------|---|------|--|--|
|           | a misread   |      |  |  |
| 4a        | <i>x</i> = 3  | B1   | Seen or implied anywhere<br>Do not accept $x = 3i$   |  |
|           | Use of $v^2 = u^2 + 2as$  | M1   | Complete method using <i>suvat</i> or<br>energy to form an equation in <i>y</i> .<br>Condone sign errors           |  |
|           | $15^2 = y^2 + 2 \times g \times 10$   | A1   | Correct unsimplified equation  |  |
|           | $y^2 = 29, y = 5.4$ or 5.39   | A1   | 2 sf or 3 sf.<br>If final answer is $y = 5.4\mathbf{j}$ do not<br>penalise inclusion of a vector a<br>second time. |  |
|           |   |      | SC allow $4/4$ for $x\mathbf{i} + y\mathbf{j} = 3\mathbf{i} + 5.4\mathbf{j}$                                       |  |
| 4         |   | [4]  |  |  |
| 4a<br>alt | <i>x</i> = 3  | B1   | Seen or implied anywhere<br>Do not accept $x = 3i$   |  |
|           | Equation for conservation of energy   | M1   | Require all 3 terms and no extras.<br>Dimensionally correct. Condone<br>sign errors. Must include <i>m</i>         |  |
|           | $\frac{1}{2}m \times (3^2 + 15^2) = mg \times 10 + \frac{1}{2}m(x^2 + y^2)$                 | A1   | Correct unsimplified equation – any equivalent form  |  |
|           | $y^2 = 29, y = 5.4$ or 5.39   | A1   | 2 sf or 3 sf.<br>If final answer is $y = 5.4j$ do not<br>penalise inclusion of a vector a<br>second time.          |  |
|           |   | [4]  |  |  |
| 4b        | Time from <i>B</i> to <i>C</i> :  | M1   | Complete method using <i>suvat</i> and their vertical speed.<br>Condone sign errors                                |  |
|           | -15 = 5.39 - gt ( $t = 2.08$ )  | Alft | Correct equation in <i>t</i> only  |  |
|           |   |      | e.g. $10 = 15t - \frac{1}{2}gt^2$  |  |
|           |   |      | ft on their 5.39 if used   |  |
|           | Horizontal distance   | DM1  | Complete method using <i>suvat</i> and   |  |
|           | $= 3t (= their \ x \times their \ t)$   |      | their x value.   |  |
|           | × ,   |      | Dependent on preceding M1  |  |
|           | (AC =) 6.2(m)  or  6.24(m)  | A1   | 2 sf or 3 sf   |  |
|           |   |      | NB Penalise over-accuracy only   |  |
|           |   | [4]  | once per question  |  |
|           |   | 141  |  |  |
|           |   | (8)  |  |  |
|           |   |      |  |  |

| 5a        | Impulse-momentum equation.   | M1        | Dimensionally correct.<br>Subtraction seen or implied.<br>Condone subtraction in wrong<br>order.  |
|-----------|--|-----------|---|
|           | (±I=)  | Al        | Or equivalent   |
|           | $(\pm \mathbf{i} -)$<br>2( $\lambda \mathbf{i} + \lambda \mathbf{j}$ )-2(4 $\mathbf{i}$ )(=(2 $\lambda$ -8) $\mathbf{i}$ +2 $\lambda \mathbf{j}$ ) | 111       | Ignore $4\sqrt{10}$ if seen here  |
|           | $( \mathbf{I} ^2 =)160 = (2\lambda - 8)^2 + (2\lambda)^2$  | DM1       | Use of Pythagoras to obtain an equation in $\lambda$ Dependent on the previous M1   |
|           | $\left(\Rightarrow 0 = \lambda^2 - 4\lambda - 12\right)$   | A1        | Or any correct unsimplified equation in $\lambda$   |
|           | $\Rightarrow (\lambda =) 6$  | A1        | Correct only.   |
|           | SC Allow 5/5 in (a) if working with -I. The  | y will lo | ose marks later.  |
|           |  | [5]       |   |
| 5a<br>alt | Form vector triangle for impulse or for momentum.  | M1        | Dimensionally correct. Must be<br>subtracting. Condone<br>subtraction in wrong order.   |
|           | Correct triangle   | A1        | $4\sqrt{10}$<br>e.g.  |
|           | $160 = 64 + 8\lambda^2 - 32\sqrt{2}\lambda \times \frac{1}{\sqrt{2}}$  | DM1       | Use of Cosine Rule to obtain an equation in $\lambda$ Dependent on the previous M1  |
|           | $\Rightarrow 0 = 8\lambda^2 - 32\lambda - 96$  | A1        | Or equivalent equation in $\lambda$   |
|           | $\Rightarrow (\lambda =) 6$  | A1        | Correct only  |
|           |  | [5]       |   |
| 5b        | $\mathbf{I} = 4\mathbf{i} + 12\mathbf{j}$  | B1ft      | Follow their $\lambda$<br>$(\mathbf{I} = (2\lambda - 8)\mathbf{i} + 2\lambda\mathbf{j})$<br>B0 for a column vector. B0 if<br>still in terms of lambda. Ignore<br>second solution for negative<br>lambda if seen |
| 5.        | 12 1/  | [1]<br>M1 | Compatives of this or realized  |
| 5c        | $\tan \theta^{\circ} = \frac{12}{4} \text{ or } \cos \theta^{\circ} = \frac{16}{4 \times 4\sqrt{10}}$  | M1        | Correct use of trig or scalar<br>product for the required angle<br>with <i>their</i> I provided both<br>components are non-zero<br>Do not allow for the reciprocal  |
|           | $\theta = 72$  | A1        | 72 or better (71.56505) from<br>correct work only<br>Ignore second solution for<br>negative lambda if seen  |
| I         |  | 1 1-1     | 1   |

| 6a  |   | rectangle                      | triangle               | lamina  | 11   |  |
|-----|---|--------------------------------|------------------------|---------|------|--|
| Jua | area  | $8ka^2$                        | $3ka^2$                | $5ka^2$ | B1   | Correct area ratio seen or implied                                   |
|     | From AD   | 4 <i>a</i>                     | 2a                     | d d     | B1   | Correct distances from <i>AD</i> or a                                |
|     |   | Ĩŭ                             | 24                     | u       |      | parallel axis seen or implied.                                       |
|     |   |                                |                        |         |      | Condone if <i>d</i> not used   |
|     | Moments   | about AD                       |                        |         | M1   | Or a parallel axis. Need all terms.                                  |
|     |   |                                |                        |         |      | Dimensionally consistent.  |
|     |   |                                |                        |         |      | Condone sign error.  |
|     | $8ka^2 \times 4a$ $26a = 5d$  | $-3ka^2 \times 2a$             | $a = 5ka^2 \times a^2$ | d       | A1   | Correct unsimplified equation  |
|     | 26a - 5d  | $\rightarrow d - \frac{26}{2}$ | a *                    |         | A1*  | Obtain given answer from correct                                     |
|     | 20u - 3u  | $\rightarrow u = 5$            | u                      |         |      | working. <b>Must obtain</b> <i>d</i> =                               |
|     |   |                                |                        |         | [5]  |  |
|     |   |                                |                        |         |      |  |
| 6b  | Moments   | about <i>PS</i>                |                        |         | M1   | Or a parallel axis. Need all terms.                                  |
|     |   |                                |                        |         |      | Dimensionally consistent.  |
|     |   |                                |                        |         |      | Must be using the 3 correctly with                                   |
|     |   |                                |                        |         |      | areas, so $5ka^2$ , $15ka^2$ , $15ka^2$ is M0.                       |
|     |   |                                |                        |         |      | Allow a slip on one value.   |
|     |   |                                |                        |         |      | Condone sign error.  |
|     | $5k \times \frac{26}{5}a + 2 \times 3 \times 4k \times 4a = (5k + 24k)\overline{x}$ |                                |                        |         | A1   | Unsimplified equation with a slip                                    |
|     | 5   |                                | (                      | )       | A 1  | on at most one value   |
|     |   |                                |                        |         | A1   | Correct unsimplified equation.<br>Allow with common factors          |
|     |   |                                |                        |         |      | cancelled  |
|     | $\overline{x} = \frac{122}{29}a$  |                                |                        |         | A1   | Correct only   |
|     | $\overline{y} = ka$   |                                |                        |         | B1   | Distance from PQ seen or implied                                     |
|     | $\tan \theta = \frac{122}{29k}$   |                                |                        |         | A1ft | Follow their $\overline{x}$ . $\left(\frac{\overline{x}}{ka}\right)$ |
|     |   |                                |                        |         | [6]  |  |
|     |   |                                |                        |         | (11) |  |
|     |   |                                |                        |         |      |  |

| 7a       | $ \begin{array}{c} D \\ 0 \\ 8a \\ V \\ 0 \\ 4a \\ 12W \\ H \end{array} $                           |                          | NB: This is a "show that" question.<br>The working must give a clear<br>indication of where the lengths in<br>the moments equation come from.<br>Check the diagram. Could be<br>resolving or using similar triangles.<br>Might have resorted to using a<br>calculator to evaluate the angles.<br>Each term should include a trig<br>ratio |  |
|----------|---|--------------------------|---|--|
|          | Moments about A   | M1                       | Or an alternative complete method<br>to form an equation in $T$ . Condone<br>sign errors and sine / cosine<br>confusion. Need all terms and<br>dimensionally consistent. (accept<br>with no $a$ )   |  |
|          | $12W \times 4a\sin\theta + W \times 8a\sin\theta = 5a \times T\sin 2\theta$                         | A1                       | Unsimplified equation with at most  |  |
|          | or $48aW\sin\theta + 8aW\sin\theta = 8aT\sin\theta$   |                          | one error   |  |
|          | $48aW\sin\theta + 8aW\sin\theta$ or   | A1                       | Correct unsimplified equation   |  |
|          | $= 3aT\cos\theta + 4aT\sin\theta$   |                          | Allow A1A0 if angle <i>DCB</i> used   |  |
|          | $\begin{pmatrix} 10 & 3 \\ 10 & 0 \end{pmatrix}$  |                          | and not in terms of $\theta$<br>If no trig in the moments equation  |  |
|          | $\left(48\times\frac{3}{5}W+8\times\frac{3}{5}W=T\times10\times\frac{3}{5}\times\frac{4}{5}\right)$ |                          | then $M0 - given answer, so no$   |  |
|          |   |                          | BOD   |  |
|          | $56W = 8T \Longrightarrow T = 7W *$   | A1*                      | Obtain given answer from correct working  |  |
|          |   | [4]                      | U   |  |
| 7b       | First equation e.g. resolve horizontally  | M1                       | Condone sign errors and sine / cosine confusion   |  |
|          | $(\pm)H = T\sin\theta \left(=\frac{21}{5}W\right)$  | A1                       | Correct unsimplified equation<br>Alt: resolving parallel to the rod:<br>$13W\cos\theta = T\cos 2\theta + R\cos\alpha$   |  |
|          | Second equation e.g. resolve vertically   | M1                       | Condone sign errors and sine / cosine confusion   |  |
|          | $(\pm)V + T\cos\theta = 13W\left(V = \frac{37}{5}W\right)$  | A1                       | Correct unsimplified equation<br>Alt resolving perpendicular to the<br>rod: $13W \sin \theta = R \sin \alpha + T \sin 2\theta$  |  |
|          | Another alternative is to use a second mor  |                          | -   |  |
|          | e.g M(C): $5a \times R \sin \alpha + W \times 3a \sin \theta = 12W$                                 | $W \times a \sin \theta$ | $h \theta$  |  |
|          | $M(B): R\sin\alpha \times 8a + T\sin 2\theta \times 3a = 12W \times 4a\sin\theta$                   |                          |   |  |
|          | $\alpha^{\circ} = \tan^{-1}\frac{3}{4} - \tan^{-1}\frac{H}{V}$                                      | DM1                      | Complete method to obtain $\alpha$<br>Dependent on the two preceding M<br>marks   |  |
|          | or $\tan^{-1}\frac{V}{H} - \tan^{-1}\frac{4}{3}$  | DIVII                    | Alt gives<br>$R \sin \alpha = \frac{27}{25}W, R \cos \alpha = \frac{211}{25}$   |  |
|          | $\alpha = 7.3$  | A1                       | 7.29205 or better. Mark 0.127<br>radians as a misread   |  |
| <u> </u> |   | [6]                      |   |  |
| 1        |   |                          |   |  |

| 8a | 6u $u$   |           |  |
|----|--|-----------|--|
|    | P<br>m<br>Q<br>km  |           |  |
|    | $\xrightarrow{2v}$ $\xrightarrow{3v}$  |           |  |
|    | Use of impact law  | M1        | Used the right way round.<br>Condone sign errors   |
|    | $\frac{3v-2v}{6u+u} = \frac{1}{3}$   | A1        | Correct unsimplified equation<br>e.g. If see just $\frac{v}{5u} = \frac{1}{3}$ assume a<br>sign slip and allow M1A0A0  |
|    | $v = \frac{7}{3}u$   | A1        | Correct only. CSO  |
|    |  | [3]       |  |
| 8b | Use of CLM<br>(or equal and opposite impulses)   | M1        | Dimensionally consistent. Need all<br>terms. Condone sign errors.<br>Condone one slip in matching<br>speeds and masses. Condone<br>consistent omission of <i>m</i> . |
|    | 6mu - kmu = 3kmv + 2mv  or<br>6u - ku = 3kv + 2v   | A1        | Correct unsimplified equation<br>Allow the marks if CLM stated<br>correctly in (a) and used here.  |
|    | $6-k = 3k \times \frac{7}{3} + 2 \times \frac{7}{3},  8k = \frac{4}{3},  k = \frac{1}{6}$  | A1        | Correct only from correct work only  |
|    |  | [3]       |  |
| 8c | This method looks at the total time betwee   | en the tv | vo collisions between $P$ and $Q$  |
|    | Speed of Q after rebound<br>= $f \times 3v (= f \times 7u)$  | B1ft      | Seen or implied<br>ft is for correct use of their v  |
|    | $t_P$ between collisions<br>= $\frac{6d}{7 \times 2v} \left( = \frac{3d}{7v} = \frac{9d}{49u} \right)$   | B1ft      | Seen or implied<br>For <i>P</i> distance $6d/7$ at $2v$<br>ft is for correct use of their <i>v</i>   |
|    | $t_Q$ between collisions $= \frac{d}{3v} + \frac{d}{7 \times 3fv}$<br>$\left(= \frac{d}{7u} + \frac{d}{49fu}\right)$   | M1        | For $Q$ distance $d$ at $3v$ and distance $d/7$ at $3vf$   |
|    | $t_{Q} = t_{P} \Longrightarrow \frac{3d}{7v} = \frac{d}{3v} + \frac{d}{21fv}$  | DM1       | Equate times and solve for <i>f</i><br>Dependent on preceding M1   |
|    | $t_{Q} = t_{P} \Longrightarrow \frac{3d}{7v} = \frac{d}{3v} + \frac{d}{21fv}$ $\frac{3}{7} = \frac{1}{3} + \frac{1}{21f},  \frac{2}{21} = \frac{1}{21f},  f = \frac{1}{2}$ | A1        | Correct only from correct working  |
|    |  | [5]       |  |
|    | See over for alternatives  |           |  |

| 8c  | This method looks at the time between the co  | ollision | between $\Omega$ and the wall and the  |
|-----|---|----------|--|
| alt | second collision between P and Q  |          | con con con a una mo wan una mo  |
|     | Speed of $Q$ after rebound  |          | Seen or implied  |
|     | $= f \times 3v (= f \times 7u)$   | B1ft     | ft is for correct use of their $v$   |
|     | Distance apart when $Q$ hits wall   |          | Seen or implied  |
|     |   | B1ft     | ft is for correct use of their v   |
|     | $= d - \frac{14u}{3} \times \frac{d}{7u} \left( = \frac{d}{3} \right)$              | Diff     | Distance moved by $Q$ – distance moved by $P$  |
|     | $t_p$ for extra distance  |          | Additional time to second  |
|     | 4d  14u (4d)  | M1       | collision = extra distance   |
|     | $=\frac{4d}{21}\div\frac{14u}{3}\left(=\frac{4d}{21}\div2v\right)$                  |          | divided by speed of P  |
|     | 4d $14u$ $d$  |          | Equate times to second collision   |
|     | $t_Q = t_P \Longrightarrow \frac{4d}{21} \div \frac{14u}{3} = \frac{d}{7} \div 7uf$ | DM1      | and solve for <i>f</i>   |
|     |   |          | Dependent on preceding M1  |
|     | $\frac{12}{3 \times 2 \times 49} = \frac{1}{49f},  f = \frac{1}{2}$                 | A1       | Correct only from correct  |
|     | $3 \times 2 \times 49$ $49f$ 2  |          | working  |
|     |   | [5]      |  |
| 8c  | This method looks at how far $Q$ travels after                                      | the rebo | bund   |
| alt | Speed of O after rehound  |          | ~  |
|     | Speed of Q after rebound<br>f(x) = f(x) f(x) f(x)                                   | B1ft     | Seen or implied  |
|     | $= f \times 3v \left(= f \times 7u\right)$  | 510      | ft is for correct use of their v   |
|     | $t_P$ between collisions $=\frac{6d}{7 \times 2v} \left(=\frac{3d}{7v}\right)$      | B1ft     |  |
|     | Distance travelled by $Q$ if $f = 1$  | M1       |  |
|     | 3d 9  |          |  |
|     | $=\frac{3d}{7v}\times 3v=\frac{9}{7}d$  |          |  |
|     | $f = \frac{\text{actual distance after rebound}}{9}$                                | M1       | This is equivalent to  |
|     | $f = \frac{9}{\frac{9}{7}d - d}$  |          | $\frac{3d}{2} \times 3v = \frac{d}{2} \times 3v + \frac{d}{21.6} \times 3v$  |
|     | $\frac{1}{7}a - a$  |          | $\frac{7v}{7v} \times \frac{3v}{3v} = \frac{3v}{3v} \times \frac{3v}{21} + \frac{1}{21} + \frac{3v}{21} + \frac{3v}$ |
|     |   |          | or $\frac{9d}{7} = d + \frac{d}{7f}$   |
|     |   |          | or $\frac{1}{7} = a + \frac{1}{7f}$  |
|     | 1   | A1       | Correct only from correct  |
|     | $=\frac{1}{2}$  |          | working  |
|     |   | [5]      |  |
| 8c  | This method looks at distances  |          |  |
| alt |   |          |  |
|     | Speed of $Q$ after rebound  | B1ft     | Seen or implied  |
|     | $= f \times 3v \left(= f \times 7u\right)$  |          | ft is for correct use of their <i>v</i>  |
|     | If $t_1$ is the time for $Q$ to the wall and $t_2$ is                               | B1ft     |  |
|     | the time between wall and second collision  |          |  |
|     | distance travelled by <i>P</i> is $(t_1 + t_2)\frac{14}{3}u$                        |          |  |
|     | 3   |          |  |
|     |   |          |  |

| $(t_1 + t_2)\frac{14}{3}u = \frac{6}{7} \times 7ut_1$ | M1  | Equate distances for $P$ and $Q$     |
|---|-----|--------------------------------------|
| Use $\frac{d}{7} = 7uf \times t_2$ and solve          | M1  |                                      |
| Obtain $f = \frac{1}{2}$                              | A1  | Correct only from correct<br>working |
|   | [5] |                                      |
|   |     |                                      |

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