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**Edexcel**

Comparison of key skills specifications 2000/2002  
with 2004 standardsX015461July 2004Issue 1

# Mark Scheme (Results)

October 2024

Pearson Edexcel International Advanced Level  
In Statistics (WST02) Paper 01

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## General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

## General Instructions for Marking

1. The total number of marks for the paper is 75.
2. The Edexcel Mathematics mark schemes use the following types of marks:
  - **M** marks: Method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
  - **A** marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
  - **B** marks are unconditional accuracy marks (independent of M marks)

Marks should not be subdivided.

### 3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes and can be used if you are using the annotation facility on ePEN:

- bod – benefit of doubt
- ft – follow through 
  - o the symbol  will be used for correct ft
- cao – correct answer only
- cso – correct solution only. There must be no errors in this part of the question to obtain this mark
- isw – ignore subsequent working
- awrt – answers which round to

- SC – special case
- oe – or equivalent (and appropriate)
- d... or dep – dependent
- indep – independent
- dp – decimal places
- sf – significant figures
- □ – The answer is printed on the paper or ag- answer given
- [ or d... – The second mark is dependent on gaining the first mark

4. All A marks are 'correct answer only' (cao), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.

5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected. If you are using the annotation facility on ePEN, indicate this action by 'MR' in the body of the script.

6. If a candidate makes more than one attempt at any question:

- a) If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
- b) If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.

7. Ignore wrong working or incorrect statements following a correct answer.

**Special notes for marking Statistics exams (for AAs only)**

- Any correct method should gain credit. If you cannot see how to apply the mark scheme but believe the method to be correct then please send to review.
- For method marks, we generally allow or condone a slip or transcription error if these are seen in an expression. We do not, however, condone or allow these errors in accuracy marks.

Comparison of key skills specifications 2000/2002 with 2004 standards X015461 July 2004 Issue 1 Question Number	Scheme		Marks
1 (a)	$X = \text{Number of items of litter found in a } 2\text{m}^2 \text{ area of the beach}$ So $X \sim \text{Po}(8)$ $P(X = 5) = \frac{e^{-8} \times 8^5}{5!}$ or $P(X \leq 5) - P(X \leq 4) = 0.1912 - 0.0996$ $= 0.09160\dots$ awrt 0.0916		M1 A1 (2)
(b)	$Y = \text{Number of face masks found in a } 5\text{m}^2 \text{ area of the beach}$ $Y \sim \text{Po}(6)$ or $P(Y \geq 5) = 1 - P(Y \leq 4) = 1 - 0.2851$ $= 0.7149$ awrt 0.715		M1 A1 (2)
(c)	$W = \text{Number of items of litter that are not face masks found in a } 20\text{m}^2 \text{ area of the beach}$ $W \sim N(56, 56)$ $P(W < 60) = P\left(Z < \frac{59.5 - 56}{\sqrt{56}}\right)$ Tables $[P(Z < 0.47)] = 0.6808$ calculator 0.68000... awrt 0.68		M1 M1 M1 A1 (4)
<b>Notes</b>			<b>Total 8</b>
(a)	<b>M1</b>	for use of $\frac{e^{-8} \lambda^5}{5!}$ or $P(X \leq 5) - P(X \leq 4)$	
	<b>A1</b>	awrt 0.0916 (correct answer scores 2 out of 2)	
(b)	<b>M1</b>	for writing or using Po(6) or for a correct probability statement $1 - P(Y \leq 4)$ or $P(Y \geq 5)$ e.g. $P(Y \geq 5) = 1 - P(Y \leq 4)$ is M0	
	<b>A1</b>	awrt 0.715 (correct answer scores 2 out of 2)	
(c)	<b>M1</b>	for writing or using N(56, 56) may be seen in standardisation	

		$\frac{x - 56}{\sqrt{56}}$ (may be implied by the standardisation $\frac{x - 56}{\sqrt{56}}$ )
	<b>M1</b>	standardising with 59.5/60/60.5, their mean and their standard deviation
	<b>M1</b>	using a continuity correction $60 + 0.5 [=60.5]$ or $60 - 0.5 [=59.5]$
	<b>A1</b>	awrt 0.68 (NB Use of exact Poisson gives 0.68617...and scores 0 out of 4)

Comparison of key skills specifications 2000/2002 with 2004 standards X015461 July 2004 Issue 1 Question Number	Scheme	Marks
2 (a)	$B\left(25, \frac{1}{5}\right)$	B1 (1)
(b)(i)	$[M =]4X - (25 - X) [= 5X - 25]$	B1
(ii)	$E(M) = '5'E(X) - '25'$	M1
	$E(X) = np = 25 \times \frac{1}{5} = 5$	M1
	$E(M) = 5 \times 5 - 25 = 0 *$	A1*
		(4)
(c)	$M \dots 30 \Rightarrow '5'X - '25' \dots 30 [\Rightarrow X \dots 11]$	M1

		$[P(X \dots '11') = 1 - P(X, '10')] = 1 - '0.9944'$	M1
		$= 0.0056$	awrt 0.0056 A1
			(3)
(d)		$Y \sim B(50, 0.5)$	
		$P(n < Y, 30) = 0.9328$	M1
		$P(Y, 30) - P(Y, n) = 0.9328$	M1
		$P(Y, n) = 0.0077$	M1
		$n = 16$	A1
			(4)
<b>Notes</b>			<b>Total 12</b>
(a)	<b>B1</b>	Correct distribution fully specified. Allow in words e.g. Binomial with $n = 25$ and $p = 0.2$ Must be seen in part (a)	
<b>Mark parts (b)(i) and (b)(ii) together</b>			
(b)(i)	<b>B1</b>	For a correct expression for $M$ Allow unsimplified	
(ii)	<b>M1</b>	For either '5'E(X) - '25' or $E(M) = 5 \times \left(25 \times \frac{1}{5}\right) - 25$ or '4'E(X) - 1('25' - E(X)) This must be an <b>expectation</b> statement with the expectation stated in symbol or in words. $5 \times 5 - 25 = 0$ or $4 \times 5 - 1 \times 20 = 0$ on its own is M0	
	<b>M1</b>	For sight of $25 \times \frac{1}{5}$ or stating $E(X) = 5$	
	<b>A1*</b>	Fully correct solution with $E(M) = 0$ stated. This may be stated in words. The answer is given so no incorrect working can be seen	
<b>SC</b>		M1M1 [Expected number of marks (per question) =] $4 \times \frac{1}{5} - 1 \times \frac{4}{5}$ A1 therefore $E(M) = 0$	
(c)	<b>M1</b>	For substitution of their $M$ into a linear inequality in terms of $X$ implied by $X \dots 11$	
	<b>M1</b>	For use of correct probability statement from their '11'	
	<b>A1</b>	awrt 0.0056 (calc 0.0055549...)	
(d)	<b>M1</b>	For a correct probability equation (implied by 2 <sup>nd</sup> M1)	
	<b>M1</b>	For $P(Y, 30) - P(Y, n) = 0.9328$ or $0.9405 - P(Y, n) = 0.9328$	
	<b>M1</b>	For $P(Y, n) = 0.0077$	
	<b>A1</b>	Cao	
<b>SC</b>		$P(n < Y, 30) = 0.9328$ $P(Y, 30) - P(Y, n-1) = 0.9328$ $P(Y, n-1) = 0.0077$ scores M1M0M1A0	
Comparison of key skills specifications	Scheme		Marks

2000/2002 with 2004 standards X015461 July 2004 Issue 1 Question Number		
3 (a)	Po(7)	B1 (1)
(b)	<b>Customers</b> enter the shop occur singly/randomly/independently/ <b>constant</b> (average) rate	B1, B1 (2)
(c)	$H_0 : \lambda = '7'$ $H_1 : \lambda \neq '7'$	B1ft (1)
(d)	$P(X_{,,} 2) = \text{awrt } 0.0073$ $P(X_{,,} 2) = \text{awrt } 0.0296$	M1
	$P(X \dots 13) = \text{awrt } 0.0270$ $P(X \dots 14) = \text{awrt } 0.0128$	M1
	$X_{,,} 2 \cup X \dots 14$	A1 (3)
(e)	$0.0073 + 0.0128 = 0.0201$	M1
	So 2.01%	A1ft (2)
(f)	12 is not in the critical region	M1
	So, there is insufficient evidence that <b>rate</b> of <b>customers</b> entering the shop has <b>changed</b>	A1 (2)
<b>Notes</b>		<b>Total 11</b>
(a)	<b>B1</b>	Correct distribution fully specified. Po(isson) and $\lambda = 7$
(b)	<b>B1, B1</b>	For two of the given assumptions (must have context of customers/people) Context only needs to be stated once. (B1B0 for one assumption in context <b>or</b> for two assumptions with no context)
(c)	<b>B1ft</b>	Both hypotheses correct. Must be attached to $H_0$ and $H_1$ in terms of $\lambda$ or $\mu$ Ft their 7 from part (a) in the hypotheses
(d)	<b>M1</b>	Use of $Po(7)$ to find the lower critical value. May be implied by either awrt 0.0073 or awrt 0.0296 seen (must be seen in part (d)) Also implied by $X=1$ or $X_{,,} 2$
	<b>M1</b>	Use of $Po(7)$ to find the upper critical value. May be implied by awrt 0.0270 or awrt 0.0128 or awrt 0.973 or awrt 0.987 seen (must be seen in part (d)) Also implied by $X=14$ or $X \dots 14$
	<b>A1</b>	$X_{,,} 2, X \dots 14$ correct CR scores 3 out of 3 but $14_{,,} X_{,,} 2$ is M1M1A0 Allow equivalent forms e.g. $X < 2, X > 13$

		Must be a CR and not a probability statement $P(X \leq 2), P(X \leq 14)$ scores M1M1A0
(e)	<b>M1</b>	Adding the two probabilities (each must be less than 0.05) for their critical region
	<b>A1ft</b>	awrt 0.0201 or awrt 2.01% ft the sum of their two selected probability tails
(f)	<b>M1</b>	For a correct comparison of 12 with their CR (or their implied CR if one is not explicitly stated), 12 is not in the CR condone $12 < '14'$ Finding $P(X = 12)$ is M0  Finding $P(X \leq 12)$ on its own is M0, they must state 12 is not in the CR
	<b>A1</b>	Correct conclusion in context. Must be a rate, e.g. number in/per 10-minute period (not number on its own). No hypotheses in part (c) then A0 Do not allow comments about the manager's claim on its own, e.g. The manager's claim is not supported. This is not a ft mark.

Comparison of key skills specifications 2000/2002 with 2004 standards X015461 July 2004 Issue 1 Question Number	Scheme	Marks		
4 (i)(a)	$\frac{b-27}{b-a} = \frac{3}{4}$ or $\frac{27-a}{b-a} = \frac{1}{4}$ and $\frac{(b-a)^2}{12} = 300$	M1M1		
	$a = 12$ and $b = 72$	A1		
		(3)		
(b)	$[4P(X < k-10) = P(X > k+20) \Rightarrow] 4\left(\frac{k-10-'12'}{72-12'}\right) = \frac{72'-(k+20)}{72-12'}$	M1		
	$4(k-22) = 52-k \Rightarrow k = 28$	A1		
		(2)		
(ii)	$L \sim U(21, 42)$	$L \sim U(0, 42)$	$S \sim U(5.25, 10.5)$	
	$\frac{L}{4} - \left(\frac{42-L}{4}\right) > 2$	$\frac{L}{4} - \left(\frac{42-L}{4}\right) > 2$ or $\left(\frac{42-L}{4}\right) - \frac{L}{4} > 2$	$S - (10.5 - S) > 2$	M1
	$L > 25$	$L < 17$ or $L > 25$	$S > 6.25$	A1

	$= (42 - '25') \times \frac{1}{21}$	$= ('17' - 0) \times \frac{1}{42} + (42 - '25') \times \frac{1}{42}$	$(10.5 - '6.25') \times \frac{1}{5.25}$	M1
	$\frac{17}{21}$ oe			A1
				(4)
	<b>Notes</b>			<b>Total 9</b>
(i)(a)	<b>M1</b>	For setting up a correct equation for the probability <b>or</b> the variance		
	<b>M1</b>	For setting up a correct equation for the probability <b>and</b> the variance		
	<b>A1</b>	For $a = 12$ and $b = 72$ (correct answers score 3 out of 3)		
(b)	<b>M1</b>	For an unsimplified equation fit their $a$ and their $b$		
	<b>A1</b>	Cao		
(ii)	<b>M1</b>	For $\frac{L}{4} - \left(\frac{42-L}{4}\right) > 2$ or $\left(\frac{42-L}{4}\right) - \frac{L}{4} > 2$ or $S - (10.5 - S) > 2$ may be seen in a probability statement allow any letter for $L$ or $S$ may be implied by $L > 25$ or $L < 17$ or $S > 6.25$		
	<b>A1</b>	$L > 25$ or $L < 17$ or $S > 6.25$ may be seen in a probability statement or implied by 2 <sup>nd</sup> M1		
	<b>M1</b>	For use of $(42 - '25') \times \frac{1}{21}$ or $('17' - 0) \times \frac{1}{42} + (42 - '25') \times \frac{1}{42}$ or $(10.5 - '6.25') \times \frac{1}{5.25}$		
	<b>A1</b>	Allow awrt 0.81		

Comparis on of key skills specificat ions 2000/200 2 with 2004 standards X015461 July 2004Issu e 1Questio n Number	Scheme	Marks
5 (a)	$\int_1^x \frac{1}{4}(3-t) dt = \frac{1}{4} \left[ 3t - \frac{t^2}{2} \right]_1^x \quad \text{or} \quad \int \frac{1}{4}(3-x) dx = \frac{1}{4} \left[ 3x - \frac{x^2}{2} \right] + C$ $\frac{1}{4} \left[ \left( 3x - \frac{x^2}{2} \right) - \left( 3 - \frac{1}{2} \right) \right] \quad \text{or} \quad \frac{1}{4} \left[ 3(1) - \frac{(1)^2}{2} \right] + C = 0 \quad \text{and} \quad C = -\frac{5}{8}$ <p>Leading to <math>\frac{1}{4} \left( 3x - \frac{x^2}{2} \right) - \frac{5}{8}</math> [for 1 „ x „ 2] *</p>	M1  A1*
(b)	$\int_2^x \frac{1}{4} dt + F(2) \quad \text{or} \quad \int \frac{1}{4} dx \quad \text{and using } + c \text{ with } F(2) = \frac{3}{8} \quad \text{or}$ $0.25(x-2) + F(2)$	M1
	$\int_3^x \frac{1}{4}(t-2) dt + F(3) \quad \text{or} \quad \int \frac{1}{4}(x-2) dx \quad \text{and using } + c \text{ with either } F(3) = \frac{5}{8} \text{ or } F(4) = 1$	M1
	$F(x) = \begin{cases} 0 & x < 1 \\ \frac{1}{4} \left( 3x - \frac{x^2}{2} \right) - \frac{5}{8} & 1 \leq x \leq 2 \\ \frac{1}{8}(2x-1) & 2 < x \leq 3 \\ \frac{1}{4} \left( \frac{x^2}{2} - 2x \right) + 1 & 3 < x \leq 4 \\ 1 & x > 4 \end{cases}$	A1 A1 B1
(c)	$P(1.2 < X < 3.1) = F(3.1) - F(1.2)$	(5)

	$\left( \frac{1}{4} \left( \frac{(3.1)^2}{2} - 2(3.1) \right) + 1 \right) - \left( \frac{1}{4} \left( 3(1.2) - \frac{(1.2)^2}{2} \right) - \frac{5}{8} \right) = \frac{89}{160}$		M1 A1
	awrt 0.556		(2)
<b>Notes</b>			<b>Total 9</b>
(a)	<b>M1</b>	For a correct method for $1 < x < 2$ Condone poor notation e.g. $\int_1^x \frac{1}{4}(3-x) dx$	
	<b>A1*</b>	A fully correct solution with substitution seen or $C$ found leading to $F(x) = \frac{1}{4} \left( 3x - \frac{x^2}{2} \right) - \frac{5}{8}$	
(b)	<b>M1</b>	For a correct method for $2 < x < 3$	
	<b>M1</b>	For a correct method for $3 < x < 4$	
	<b>A1</b>	Third line correct including inequality. Allow $<$ instead of $\leq$	
	<b>A1</b>	Fourth line correct including inequality. Allow $<$ instead of $\leq$	
	<b>B1</b>	First and fifth line correct. Allow "otherwise" for the range on the first or fifth line but not both	
(c)	<b>M1</b>	For use of $F(3.1) - F(1.2)$ from the correct lines of their $F(x)$ allow ft on their 4 <sup>th</sup> line $\frac{1}{2} \times \frac{7}{10} \times 0.8 + 1 \times \frac{1}{4} + \frac{1}{2} \times \frac{21}{40} \times 0.1$ or correct use of $f(x)$ or area e.g.	
	<b>A1</b>	For $\frac{89}{160}$ oe or awrt 0.556 NB: Use of $F(3.1)$ with $\frac{1}{8}(2x-1)$ for $2 < x < 3$ gives 0.555 and scores M0A0	
Comparis on of key skills specificat ions 2000/200 2 with 2004 standards X015461 July 2004Issu e 1Questio n Number	Scheme		Marks
6 (a)	Box A: $P(1) = \frac{1}{4}$ $P(2) = \frac{3}{4}$	Box B: $P(2) = \frac{1}{5}$ $P(5) = \frac{4}{5}$	B1
	Totals ( $T$ ) 5, 6, 8, 9, 11, 12		B1
	(1, 2, 2) (1, 2, 5) (1, 5, 5) (2, 2, 2) (2, 2, 5) (2, 5, 5)	[(1, 5, 2)] [(2, 5, 2)]	B1
	$[P(T = 5) =] \frac{1}{4} \times \frac{1}{5} \times \frac{1}{5} [ = \frac{1}{100} ]$	$[P(T = 6) =] \frac{3}{4} \times \frac{1}{5} \times \frac{1}{5} = [ \frac{3}{100} ]$	M1
			M1

$[P(T = 8) = ] 2 \times \frac{1}{4} \times \frac{1}{5} \times \frac{4}{5} = \left[ \frac{8}{100} \right]$	$[P(T = 9) = ] 2 \times \frac{3}{4} \times \frac{1}{5} \times \frac{4}{5} = \left[ \frac{24}{100} \right]$	M1														
$[P(T = 11) = ] \frac{1}{4} \times \frac{4}{5} \times \frac{4}{5} = \left[ \frac{16}{100} \right]$	$[P(T = 12) = ] \frac{3}{4} \times \frac{4}{5} \times \frac{4}{5} = \left[ \frac{48}{100} \right]$															
<table border="1"> <tr> <td><math>t</math></td> <td>5</td> <td>6</td> <td>8</td> <td>9</td> <td>11</td> <td>12</td> </tr> <tr> <td><math>P(T = t)</math></td> <td><math>\frac{1}{100}</math></td> <td><math>\frac{3}{100}</math></td> <td><math>\frac{8}{100} \left[ = \frac{2}{25} \right]</math></td> <td><math>\frac{24}{100} \left[ = \frac{6}{25} \right]</math></td> <td><math>\frac{16}{100} \left[ = \frac{4}{25} \right]</math></td> <td><math>\frac{48}{100} \left[ = \frac{12}{25} \right]</math></td> </tr> </table>		$t$	5	6	8	9	11	12	$P(T = t)$	$\frac{1}{100}$	$\frac{3}{100}$	$\frac{8}{100} \left[ = \frac{2}{25} \right]$	$\frac{24}{100} \left[ = \frac{6}{25} \right]$	$\frac{16}{100} \left[ = \frac{4}{25} \right]$	$\frac{48}{100} \left[ = \frac{12}{25} \right]$	A1
$t$	5	6	8	9	11	12										
$P(T = t)$	$\frac{1}{100}$	$\frac{3}{100}$	$\frac{8}{100} \left[ = \frac{2}{25} \right]$	$\frac{24}{100} \left[ = \frac{6}{25} \right]$	$\frac{16}{100} \left[ = \frac{4}{25} \right]$	$\frac{48}{100} \left[ = \frac{12}{25} \right]$										
		(7)														

(b)	$m = 2$ $m = 5$	B1						
	$[P(M = 2) = ] \frac{1}{100} + \frac{8}{100} + \frac{3}{100} + \frac{24}{100} = \left[ \frac{36}{100} \right]$	M1						
	$[P(M = 5) = ] \frac{16}{100} + \frac{48}{100} = \left[ \frac{64}{100} \right]$ or $P(M = 5) = 1 - P(M = 2)$	M1						
	<table border="1"> <tr> <td><math>m</math></td> <td>2</td> <td>5</td> </tr> <tr> <td><math>P(M = m)</math></td> <td><math>\frac{36}{100}</math></td> <td><math>\frac{64}{100}</math></td> </tr> </table>	$m$	2	5	$P(M = m)$	$\frac{36}{100}$	$\frac{64}{100}$	A1
$m$	2	5						
$P(M = m)$	$\frac{36}{100}$	$\frac{64}{100}$						
		(4)						

<b>Notes</b>		<b>Total 11</b>
(a)	<b>B1</b>	All 4 correct probabilities – may be seen in an equation
	<b>B1</b>	All 6 totals correct with no extras (ignore units if stated) (condone 8 or 9 listed twice)
	<b>B1</b>	All 6 basic combinations correct, either seen or used (implied by the 3 <sup>rd</sup> M1 mark) Condone any permutation of the 6 basic combinations for this mark
	<b>M1</b>	Correct method for <b>one</b> probability (ft their probabilities)
	<b>M1</b>	Correct method for <b>five</b> probabilities (ft their probabilities)
	<b>M1</b>	Correct method for all <b>six</b> probabilities (ft their probabilities)
	<b>A1</b>	cao Need not be in a table but probabilities must be attached to the correct total
(b)	<b>B1</b>	For both values of $m$ (no extras) If $m = 1$ is stated it must be stated that its probability is 0
	<b>M1</b>	Ft part (a) For a correct method to find $P(M = '2')$ For this mark there must only be 2 probability calculations
	<b>M1</b>	Ft part (a) For a correct method to find $P(M = '5')$ For this mark there must only be 2 probability calculations
	<b>A1</b>	cao Need not be in a table but probabilities must be attached to the correct total

Comparison of key skills specifications 2000/2002 with 2004 standards X015461 July 2004 Issue 1 Question Number	Scheme	Marks
7 (a)	$\frac{1}{2} \times 8 \times 4a = 1 \Rightarrow a = \frac{1}{16} *$ or $\int_{[0]}^{[4]} ax \, dx = 0.5 \Rightarrow \left[ \frac{ax^2}{2} \right]_0^4 = 0.5 \Rightarrow a = \frac{1}{16} *$	B1*  (1)
(b) (i)	(By symmetry) $b = -\frac{1}{16}$	B1
(ii)	At (8, 0) $0 = -\frac{1}{16} \times 8 + c \Rightarrow c = \frac{1}{2}$ or at (4, 0.25) $0.25 = -\frac{1}{16} \times 4 + c \Rightarrow c = \frac{1}{2}$	M1 A1  (3)
(c)	$E(X) = 4$	B1
	$E(X^2) = \int_0^4 x^2 \left( \frac{1}{16} x \right) dx + \int_4^8 x^2 \left( -\frac{1}{16} x + \frac{1}{2} \right) dx$	M1
	$= \frac{1}{64} [x^4]_0^4 + \left[ -\frac{1}{64} x^4 + \frac{1}{6} x^3 \right]_4^8$	A1ft
	$= 4 + \left[ \left( -64 + \frac{256}{3} \right) - \left( -4 + \frac{32}{3} \right) \right] \left[ = \frac{56}{3} \right]$	dM1A1
	$\text{Var}(X) = \frac{56}{3} - 4^2 = \frac{8}{3} *$	A1*  (6)
(d)	$\frac{1}{2} \times Q_1 \times \frac{1}{16} \times Q_1 = \frac{1}{4}$ or $\int_0^{Q_1} \frac{1}{16} x \, dx = 0.25 \rightarrow \frac{Q_1^2}{32} = 0.25$	M1
	$Q_1 = \sqrt{8} = 2.828\dots$ or $Q_3 = 8 - \sqrt{8} = 5.171\dots$	awrt 2.83 or awrt 5.17 A1
	$Q_1 = \sqrt{8} = 2.828\dots$ and $Q_3 = 8 - \sqrt{8} = 5.171\dots$	awrt 2.83 and awrt 5.17 A1
		(3)
(e)	50% lies between $Q_1$ and $Q_3$	

		$P\left('4' - \sqrt{\frac{8}{3}} < X < '4' + \sqrt{\frac{8}{3}}\right) = P(2.37 < X < 5.63)$	M1
		Statistician's claim: as this is outside $Q_1$ and $Q_3$ , $> 0.5$ / statistician's claim is correct* or $P(2.37 < X < 5.63) = 0.6498... > 0.5$ / statistician's claim is correct*	A1*
			(2)
		<b>Notes</b>	<b>Total 15</b>
(a)	<b>B1*</b>	$\frac{1}{2} \times 4 \times 4a = \frac{1}{2} \Rightarrow a = \frac{1}{16}$ Allow any correct equivalent method. E.g. integration, use of gradients, etc. Answer is given so a complete correct method with no incorrect working must be seen	
(b)	<b>B1</b>	Cao	
	<b>M1</b>	Use of equation of line to find $c$ e.g. $y - 0 = -\frac{1}{16}(x - 8)$ or use of integration or any valid method	
	<b>A1</b>	Cao correct answer scores M1A1	
(c)	<b>B1</b>	For $E(X) = 4$ This may be seen at any point in the solution	
	<b>M1</b>	For use of $\int x^2 f(x) dx$ $x^n \rightarrow x^{n+1}$ for both parts of pdf (ignore limits) ft their values of $b$ and $c$	
	<b>A1ft</b>	For correct integration of <b>either</b> of the 2 parts, ft their values of $b$ and $c$	
	<b>depM1</b>	For use of correct limits in <b>either</b> part (dep on previous M1) $\frac{44}{3}$ may be implied by sight of 4 or $\frac{56}{3}$ but <b>not</b> implied by $\frac{56}{3}$ allow ft on their values of $b$ and $c$ which you may need to check	
	<b>A1</b>	For complete correct substitution $4 + \left[ \left( -64 + \frac{256}{3} \right) - \left( -4 + \frac{32}{3} \right) \right]$ or $\frac{56}{3}$ allow $= 4 + \frac{44}{3}$	
	<b>A1*</b>	Answer is given so need to see use of $\text{Var}(X) = E(X^2) - E(X)^2 = \frac{8}{3}$ with values substituted	
(d)	<b>M1</b>	For correct method for either $Q_1$ or $Q_3$ $\frac{1}{2} \times Q_1 \times \frac{1}{16} \times Q_1 = \frac{1}{4}$ e.g. $\int_0^{Q_1} \frac{1}{16} x dx = 0.25 \rightarrow \frac{Q_1^2}{32} = 0.25$	
	<b>A1</b>	For either awrt 2.83 allow $\sqrt{8}$ oe or awrt 5.17 allow $8 - \sqrt{8}$ oe	
	<b>A1</b>	For either awrt 2.83 allow $\sqrt{8}$ oe and awrt 5.17 allow $8 - \sqrt{8}$ oe	
(e)	<b>M1</b>	For use of $P(\mu - \sigma < X < \mu + \sigma)$ ft their $\mu$ implied by awrt 2.37 and awrt 5.63	
	<b>A1*</b>	Must state that this $> 0.5$ as it is outside $Q_1$ and $Q_3$	

		Allow '2.83' > '2.37' and '5.16' < '5.63' <b>or</b> a correct probability calculated awrt 0.65 Answer is given so no incorrect working can be seen. If their values are not consistent with the statistician's claim, then A0 here.
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